

---

**pyRVEA**

***Release 0.1***

**Bhupinder Saini**

**May 01, 2019**



# CONTENTS

<b>1 README</b>	<b>1</b>
1.1 Requirements: . . . . .	1
1.2 Installation process: . . . . .	1
1.3 See the details of RVEA in the following paper . . . . .	1
<b>2 pyRVEA package</b>	<b>3</b>
2.1 pyRVEA.EAs . . . . .	3
2.2 pyRVEA.OtherTools . . . . .	5
2.3 pyRVEA.Population . . . . .	9
2.4 pyRVEA.Problem package . . . . .	11
2.5 pyRVEA.Recombination package . . . . .	12
2.6 pyRVEA.Selection package . . . . .	12
<b>Python Module Index</b>	<b>15</b>



---

**CHAPTER  
ONE**

---

**README**

Binder

The python version reference vector guided evolutionary algorithm.

Currently supported: Multi-objective minimization with visualization and interaction support. Preference is accepted as a reference point.

To test the code, open the [binder link](#) and read example.ipynb.

Read the documentation here

## 1.1 Requirements:

- Python 3.6 or up
- Poetry dependency manager

## 1.2 Installation process:

- Download and extract the code
- Create a new virtual environment for the project
- Run `poetry install --no-dev` in the activated virtual environment to install the packages necessary to run the code.
- If you want to take part in the development process, run `poetry install` instead.

## 1.3 See the details of RVEA in the following paper

R. Cheng, Y. Jin, M. Olhofer and B. Sendhoff, A Reference Vector Guided Evolutionary Algorithm for Many-objective Optimization, IEEE Transactions on Evolutionary Computation, 2016

The source code of pyRVEA is implemented by Bhupinder Saini

If you have any questions about the code, please contact:

Bhupinder Saini: [bhupinder.s.saini@jyu.fi](mailto:bhupinder.s.saini@jyu.fi) Project researcher at University of Jyväskylä.



## PYRVEA PACKAGE

### 2.1 pyRVEA.EAs

#### 2.1.1 pyRVEA.EAs.NSGAIII module

```
class pyRVEA.EAs.NSGAIII(population: Population, EA_parameters: dict = None)
    Bases: pyRVEA.EAs.baseEA.BaseDecompositionEA

    Python Implementation of NSGA-III. Based on the pymoo package.

    [description]

    select (population: Population)
        Describe a selection mechanism. Return indices of selected individuals.

        Parameters population (Population) – Contains the current population and problem in-
            formation.

        Returns List of indices of individuals to be selected.

        Return type list

    set_params (population: Population = None, population_size: int = None, lattice_resolution:
        int = None, interact: bool = True, a_priori_preference: bool = False, genera-
        tions_per_iteration: int = 100, iterations: int = 10, plotting: bool = True)
        Set up the parameters. Save in self.params
```

#### 2.1.2 pyRVEA.EAs.RVEA module

```
class pyRVEA.EAs.RVEA(population: Population, EA_parameters: dict = None)
    Bases: pyRVEA.EAs.baseEA.BaseDecompositionEA
```

The python version reference vector guided evolutionary algorithm.

See the details of RVEA in the following paper

R. Cheng, Y. Jin, M. Olhofer and B. Sendhoff, A Reference Vector Guided Evolutionary Algorithm for Many-objective Optimization, IEEE Transactions on Evolutionary Computation, 2016

The source code of pyRVEA is implemented by Bhupinder Saini

If you have any questions about the code, please contact:

Bhupinder Saini: [bhupinder.s.saini@jyu.fi](mailto:bhupinder.s.saini@jyu.fi)

Project researcher at University of Jyväskylä.

**select** (*population*: Population)

Describe a selection mechanism. Return indices of selected individuals.

# APD Based selection. # This is different from the paper. # params.genetations != total number of generations. This is a compromise. Also this APD uses an archived ideal point, rather than current, potentially worse ideal point.

**Parameters** **population** (Population) – Population information**Returns** list: Indices of selected individuals.**Return type** list**set\_params** (*population*: Population = None, *population\_size*: int = None, *lattice\_resolution*: int = None, *interact*: bool = False, *a\_priori\_preference*: bool = False, *generations\_per\_iteration*: int = 100, *iterations*: int = 10, *Alpha*: float = 2, *plotting*: bool = True)

Set up the parameters. Save in RVEA.params. Note, this should be changed to align with the current structure.

**Parameters**

- **population** (Population) – Population object
- **population\_size** (int) – Population Size
- **lattice\_resolution** (int) – Lattice resolution
- **interact** (bool) – bool to enable or disable interaction. Enabled if True
- **a\_priori\_preference** (bool) – similar to interact
- **generations\_per\_iteration** (int) – Number of generations per iteration.
- **iterations** (int) – Total Number of iterations.
- **Alpha** (float) – The alpha parameter of APD selection.
- **plotting** (bool) – Useless really.

## 2.1.3 pyRVEA.EAs.baseEA module

**class** pyRVEA.EAs.baseEA.**BaseDecompositionEA** (*population*: Population, *EA\_parameters*: dict = None)Bases: *pyRVEA.EAs.baseEA.BaseEA*

This class provides the basic structure for decomposition based Evolutionary algorithms, such as RVEA or NSGA-III.

**continue\_evolution** () → bool

Checks whether the current iteration should be continued or not.

**continue\_iteration** ()

Checks whether the current iteration should be continued or not.

**select** (*population*) → list

Describe a selection mechanism. Return indices of selected individuals.

**Parameters** **population** (Population) – Contains the current population and problem information.**Returns** List of indices of individuals to be selected.**Return type** list

---

```
class pyRVEA.EAs.baseEA.BaseEA
```

Bases: object

This class provides the basic structure for Evolutionary algorithms.

```
set_params()
```

Set up the parameters. Save in self.params

## 2.2 pyRVEA.OtherTools

### 2.2.1 pyRVEA.OtherTools.IsNotebook module

```
pyRVEA.OtherTools.IsNotebook.IsNotebook() → bool
```

Checks if the current environment is a Jupyter Notebook or a console.

**Returns** True if notebook. False if console

**Return type** bool

### 2.2.2 pyRVEA.OtherTools.ReferenceVectors module

```
class pyRVEA.OtherTools.ReferenceVectors.ReferenceVectors(lattice_resolution: int,  
number_of_objectives: int, creation_type: str =  
'Uniform', vector_type:  
str = 'Spherical',  
ref_point: list = None)
```

Bases: object

Class object for reference vectors.

```
adapt(fitness: numpy.ndarray)
```

Adapt reference vectors. Then normalize.

**Parameters** **fitness** (np.ndarray) –

```
add_edge_vectors()
```

Add edge vectors to the list of reference vectors.

Used to cover the entire orthant when preference information is provided.

```
interactive_adapt_1(ref_point, translation_param=0.2)
```

Adapt reference vectors linearly towards a reference point. Then normalize.

The details can be found in the following paper: Hakanen, Jussi & Chugh, Tinkle & Sindhya, Karthik & Jin, Yaochu & Miettinen, Kaisa. (2016). Connections of Reference Vectors and Different Types of Preference Information in Interactive Multiobjective Evolutionary Algorithms.

**Parameters**

- **ref\_point** –

- **translation\_param** – (Default value = 0.2)

```
neighbouring_angles() → numpy.ndarray
```

Calculate neighbouring angles for normalization.

```
normalize()
```

Normalize the reference vectors to a unit hypersphere.

**slow\_interactive\_adapt** (*ref\_point*)

Basically a wrapper around rotate\_toward. Slowly rotate ref vectors toward ref\_point. Return a boolean value to tell if the ref\_point has been reached.

**Parameters** **ref\_point** (*list or np.ndarray*) – The reference vectors will slowly move towards the ref\_point.

**Returns** True if ref\_point has been reached. False otherwise.

**Return type** boolean

pyRVEA.OtherTools.ReferenceVectors.**householder** (*vector*)

Return reflection matrix via householder transformation.

pyRVEA.OtherTools.ReferenceVectors.**normalize** (*vectors*)

Normalize a set of vectors.

The length of the returned vectors will be unity.

**Parameters** **vectors** (*np.ndarray*) – Set of vectors of any length, except zero.

pyRVEA.OtherTools.ReferenceVectors.**rotate** (*initial\_vector, rotated\_vector, other\_vectors*)

Calculate the rotation matrix that rotates the initial\_vector to the rotated\_vector. Apply that rotation on other\_vectors and return. Uses Householder reflections twice to achieve this.

pyRVEA.OtherTools.ReferenceVectors.**rotate\_toward** (*initial\_vector, final\_vector, other\_vectors, degrees: float = 5*)

Rotate other\_vectors (with the centre at initial\_vector) towards final\_vector by an angle degrees.

**Parameters**

- **initial\_vector** (*np.ndarray*) – Centre of the vectors to be rotated.
- **final\_vector** (*np.ndarray*) – The final position of the center of other\_vectors.
- **other\_vectors** (*np.ndarray*) – The array of vectors to be rotated
- **degrees** (*float, optional*) – The amount of rotation (the default is 5)

**Returns**

- **rotated\_vectors** (*np.ndarray*) – The rotated vectors
- **reached** (*bool*) – True if final\_vector has been reached

pyRVEA.OtherTools.ReferenceVectors.**shear** (*vectors, degrees: float = 5*)

Shear a set of vectors lying on the plane z=0 towards the z-axis, such that the resulting vectors ‘degrees’ angle away from the z axis.

z is the last element of the vector, and has to be equal to zero.

**Parameters**

- **vectors** (*numpy.ndarray*) – The final element of each vector should be zero.
- **degrees** (*float, optional*) – The angle that the resultant vectors make with the z axis. Unit is radians. (the default is 5)

## 2.2.3 pyRVEA.OtherTools.newRV module

### 2.2.4 pyRVEA.OtherTools.plotlyanimate module

```
pyRVEA.OtherTools.plotlyanimate.animate_2d_init_(data: Union[numpy.ndarray, pandas.core.frame.DataFrame, list], filename: str) → dict
```

Initiate a 2D scatter animation.

Only for 2D data.

#### Parameters

- **data** (*Union[np.ndarray, pd.DataFrame, list]*) – Objective values
- **filename** (*str*) – Name of the file to which plot is saved

**Returns** Plotly Figure Object

**Return type** dict

```
pyRVEA.OtherTools.plotlyanimate.animate_2d_next_(data: Union[numpy.ndarray, pandas.core.frame.DataFrame, list], figure: dict, filename: str, generation: int) → dict
```

Plot the next set of individuals in a 2D scatter animation.

#### Parameters

- **data** (*Union[np.ndarray, pd.DataFrame, list]*) – The objective values to be plotted
- **figure** (*dict*) – Plotly figure object compatible dict
- **filename** (*str*) – Name of the file to which the plot is saved
- **generation** (*int*) – Iteration Number

**Returns** Plotly Figure Object

**Return type** dict

```
pyRVEA.OtherTools.plotlyanimate.animate_3d_init_(data: Union[numpy.ndarray, pandas.core.frame.DataFrame, list], filename: str) → dict
```

Plot the first (or zeroth) iteration of a population.

Intended as a frames object. Plots Scatter 3D data.

#### Parameters

- **data** (*Union[np.ndarray, pd.DataFrame, list]*) – Contains the data to be plotted. Each row is an individual's objective values.
- **filename** (*str*) – Contains the name of the file to which the plot is saved.

**Returns** Plotly figure object

**Return type** dict

```
pyRVEA.OtherTools.plotlyanimate.animate_3d_next_(data: Union[numpy.ndarray, pandas.core.frame.DataFrame, list], figure: dict, filename: str, generation: int) → dict
```

Plot the next set of individuals in an animation.

Plots scatter for 3D data.

**Parameters**

- **data** (*Union[np.ndarray, pd.DataFrame, list]*) – The objective values to be plotted
- **figure** (*dict*) – Plotly figure object compatible dict
- **filename** (*str*) – Name of the file to which the plot is saved
- **generation** (*int*) – Iteration Number

**Returns** Plotly Figure Object

**Return type** dict

```
pyRVEA.OtherTools.plotlyanimate.animate_init_(data: Union[numpy.ndarray, pandas.core.frame.DataFrame, list], filename: str) → dict
```

Plot the first (or zeroth) iteration of a population.

Intended as a frames object. Plots Scatter for 2D and 3D data. Plots parallel coordinate plot for higher dimensional data.

**Parameters**

- **data** (*Union[np.ndarray, pd.DataFrame, list]*) – Contains the data to be plotted. Each row is an individual's objective values.
- **filename** (*str*) – Contains the name of the file to which the plot is saved.

**Returns** Plotly figure object

**Return type** dict

```
pyRVEA.OtherTools.plotlyanimate.animate_next_(data: Union[numpy.ndarray, pandas.core.frame.DataFrame, list], figure: dict, filename: str, generation: int) → dict
```

Plot the next set of individuals in an animation.

Plots scatter for 2D and 3D data, parallel coordinate plot for 4D and up.

**Parameters**

- **data** (*Union[np.ndarray, pd.DataFrame, list]*) – The objective values to be plotted
- **figure** (*dict*) – Plotly figure object compatible dict
- **filename** (*str*) – Name of the file to which the plot is saved
- **generation** (*int*) – Iteration Number

**Returns** Plotly Figure Object

**Return type** dict

```
pyRVEA.OtherTools.plotlyanimate.animate_parallel_coords_init_(data: Union[numpy.ndarray, pandas.core.frame.DataFrame, list], filename: str) → dict
```

Plot the first (or zeroth) iteration of a population.

Intended as a frames object. Plots parallel coordinate plot for >3D data.

#### Parameters

- **data** (*Union[np.ndarray, pd.DataFrame, list]*) – Contains the data to be plotted. Each row is an individual's objective values.
- **filename** (*str*) – Contains the name of the file to which the plot is saved.

#### Returns

Plotly figure object

#### Return type

dict

```
pyRVEA.OtherTools.plotlyanimate.animate_parallel_coords_next_(data:  
                                         Union[numpy.ndarray,  
pan-  
das.core.frame.DataFrame,  
list], figure: dict,  
filename: str,  
generation: int)  
→ dict
```

Plot the next set of individuals in an animation.

Plots parallel coordinate plot for 4D and up.

#### Parameters

- **data** (*Union[np.ndarray, pd.DataFrame, list]*) – The objective values to be plotted
- **figure** (*dict*) – Plotly figure object compatible dict
- **filename** (*str*) – Name of the file to which the plot is saved
- **generation** (*int*) – Iteration Number

#### Returns

Plotly Figure Object

#### Return type

dict

```
pyRVEA.OtherTools.plotlyanimate.test()  
pyRVEA.OtherTools.plotlyanimate.test2()
```

## 2.2.5 pyRVEA.OtherTools.symmetric\_vectors module

## 2.3 pyRVEA.Population

### 2.3.1 pyRVEA.Population.Population module

```
class pyRVEA.Population.Population.Population(problem: baseProblem, assign_type: str  
                                               = 'RandomAssign', plotting: bool = True,  
                                               *args)
```

Bases: object

Define the population.

```
add(new_pop: numpy.ndarray)
```

Evaluate and add individuals to the population. Update ideal and nadir point.

**Parameters** **new\_pop** (*np.ndarray*) – Decision variable values for new population.

**append\_individual** (*ind: numpy.ndarray*)

Evaluate and add individual to the population.

**Parameters** *ind (np.ndarray)* –**create\_new\_individuals** (*design: str = 'LHSDesign', pop\_size: int = None, decision\_variables=None*)

Create, evaluate and add new individuals to the population. Initiate Plots.

The individuals can be created randomly, by LHS design, or can be passed by the user.

**Parameters**

- **design** (*str, optional*) – Describe the method of creation of new individuals. “RandomDesign” creates individuals randomly. “LHSDesign” creates individuals using Latin hypercube sampling.
- **pop\_size** (*int, optional*) – Number of individuals in the population. If none, some default population size based on number of objectives is chosen.
- **decision\_variables** (*numpy array or list, optional*) – Pass decision variables to be added to the population.

**eval\_fitness ()**

Calculate fitness based on objective values. Fitness = obj if minimized.

**evaluate\_individual** (*ind: numpy.ndarray*)

Evaluate individual.

Returns objective values, constraint violation, and fitness.

**Parameters** *ind (np.ndarray)* –**evolve** (*EA: BaseEA = None, EA\_parameters: dict = None*) → Population

Evolve the population with interruptions.

Evolves the population based on the EA sent by the user.

**Parameters**

- **EA** ("BaseEA") – Should be a derivative of BaseEA (Default value = None)
- **EA\_parameters** (*dict*) – Contains the parameters needed by EA (Default value = None)

**hypervolume** (*ref\_point*)

Calculate hypervolume. Uses package pygmo. Add checks to prevent errors.

**Parameters** *ref\_point* –**keep** (*indices: list*)

Remove individuals from population which are not in “indices”.

**Parameters** *indices (list)* – Indices of individuals to keep**mate ()**

Conduct crossover and mutation over the population.

Conduct simulated binary crossover and bounded polynominal mutation.

**non\_dominated ()**

Fix this. check if nd2 and nds mean the same thing

**plot\_init\_()**

Initialize animation objects. Return figure

---

**plot\_objectives** (*iteration: int*)  
 Plot the objective values of individuals in notebook. This is a hack.

**Parameters** **iteration** (*int*) – Iteration count.

**update\_ideal\_and\_nadir** (*new\_objective\_vals: list = None*)  
 Updates self.ideal and self.nadir in the fitness space.  
 Uses the entire population if new\_objective\_vals is none.

**Parameters** **new\_objective\_vals** (*list, optional*) – Objective values for a newly added individual (the default is None, which calculated the ideal and nadir for the entire population.)

## 2.4 pyRVEA.Problem package

### 2.4.1 Submodules

#### 2.4.2 pyRVEA.Problem.baseProblem module

```
class pyRVEA.Problem.baseProblem.baseProblem(name=None, num_of_variables=None, num_of_objectives=None, num_of_constraints=0, upper_limits=1, lower_limits=0)
```

Bases: `object`

Base class for the problems.

**constraints** (*decision\_variables*)

Accept a sample and/or corresponding objective values.

**Parameters** **decision\_variables** –

**objectives** (*decision\_variables*)

Accept a sample. Return Objective values.

**Parameters** **decision\_variables** –

**update()**

Update the problem based on new information.

#### 2.4.3 pyRVEA.Problem.testProblem module

```
class pyRVEA.Problem.testProblem.testProblem(name=None, num_of_variables=None, num_of_objectives=None, num_of_constraints=0, upper_limits=1, lower_limits=0)
```

Bases: `pyRVEA.Problem.baseProblem.baseProblem`

Defines the problem.

**constraints** (*decision\_variables, objective\_variables*)

Calculate constraint violation.

**Parameters**

- **decision\_variables** –
- **objective\_variables** –

**objectives** (*decision\_variables*) → list  
Use this method to calculate objective functions.

Parameters **decision\_variables** –

## 2.5 pyRVEA.Recombination package

### 2.5.1 Module contents

## 2.6 pyRVEA.Selection package

### 2.6.1 Submodules

#### 2.6.2 pyRVEA.Selection.APD\_select module

pyRVEA.Selection.APD\_select.**APD\_select** (*fitness*: list, *vectors*: ReferenceVectors, *penalty\_factor*: float, *ideal*: list = None)  
Select individuals for mating on basis of Angle penalized distance.

Parameters

- **fitness** (list) – Fitness of the current population.
- **vectors** (ReferenceVectors) – Class containing reference vectors.
- **penalty\_factor** (float) – Multiplier of angular deviation from Reference vectors. See RVEA paper for details.
- **ideal** (list) – ideal point for the population. Uses the min fitness value if None.

Returns A list of indices of the selected individuals.

Return type [type]

#### 2.6.3 pyRVEA.Selection.NSGAIII\_select module

pyRVEA.Selection.NSGAIII\_select.**NSGAIII\_select** (*fitness*: list, *ref\_dirs*: ReferenceVectors, *ideal\_point*: list = None, *worst\_point*: list = None, *extreme\_points*: list = None, *n\_survive*: int = None)

pyRVEA.Selection.NSGAIII\_select.**associate\_to\_niches** (*F*, *ref\_dirs*, *ideal\_point*, *nadir\_point*, *utopian\_epsilon*=0.0)

pyRVEA.Selection.NSGAIII\_select.**calc\_niche\_count** (*n Niches*, *niche\_of\_individuals*)

pyRVEA.Selection.NSGAIII\_select.**calc\_perpendicular\_distance** (*N*, *ref\_dirs*)

pyRVEA.Selection.NSGAIII\_select.**get\_extreme\_points\_c** (*F*, *ideal\_point*, *extreme\_points*=None)

Taken from pymoo

pyRVEA.Selection.NSGAIII\_select.**get\_nadir\_point** (*extreme\_points*, *ideal\_point*, *worst\_point*, *worst\_of\_front*, *worst\_of\_population*)

```
pyRVEA.Selection.NSGAIII_select.niching(F, n_remaining, niche_count,  
                                         niche_of_individuals, dist_to_niche)
```



## PYTHON MODULE INDEX

### p

pyrvea.EAs.baseEA, 4  
pyrvea.EAs.NSGAIII, 3  
pyrvea.EAs.RVEA, 3  
pyrvea.OtherTools.IsNotebook, 5  
pyrvea.OtherTools.plotlyanimate, 7  
pyrvea.OtherTools.ReferenceVectors, 5  
pyrvea.Population.Population, 9  
pyrvea.Problem.baseProblem, 11  
pyrvea.Problem.testProblem, 11  
pyrvea.Recombination, 12  
pyrvea.Selection.APD\_select, 12  
pyrvea.Selection.NSGAIII\_select, 12



# INDEX

## A

adapt () (*pyRVEA.OtherTools.ReferenceVectors.ReferenceVectors method*), 5  
add () (*pyRVEA.Population.Population Population method*), 9  
add\_edge\_vectors ()  
    (*pyRVEA.OtherTools.ReferenceVectors.ReferenceVectors method*), 5  
animate\_2d\_init\_ ()     (*in module pyRVEA.OtherTools.plotlyanimate*), 7  
animate\_2d\_next\_ ()     (*in module pyRVEA.OtherTools.plotlyanimate*), 7  
animate\_3d\_init\_ ()     (*in module pyRVEA.OtherTools.plotlyanimate*), 7  
animate\_3d\_next\_ ()     (*in module pyRVEA.OtherTools.plotlyanimate*), 7  
animate\_init\_ ()     (*in module pyRVEA.OtherTools.plotlyanimate*), 8  
animate\_next\_ ()     (*in module pyRVEA.OtherTools.plotlyanimate*), 8  
animate\_parallel\_coords\_init\_ ()     (*in module pyRVEA.OtherTools.plotlyanimate*), 8  
animate\_parallel\_coords\_next\_ ()     (*in module pyRVEA.OtherTools.plotlyanimate*), 9  
APD\_select ()     (*in module pyRVEA.Selection.APD\_select*), 12  
append\_individual ()  
    (*pyRVEA.Population.Population Population method*), 9  
associate\_to\_niches ()     (*in module pyRVEA.Selection.NSGAIII\_select*), 12

## B

BaseDecompositionEA     (*class pyRVEA.EAs.baseEA*), 4  
BaseEA (*class in pyRVEA.EAs.baseEA*), 4  
baseProblem     (*class pyRVEA.Problem.baseProblem*), 11

## C

calc\_niche\_count ()     (*in module pyRVEA.Selection.NSGAIII\_select*), 12

calc\_perpendicular\_distance ()     (*in module pyRVEA.Selection.NSGAIII\_select*), 12  
constraints () (*pyRVEA.Problem.baseProblem.baseProblem method*), 11  
constraints () (*pyRVEA.Problem.testProblem.testProblem method*), 11  
continue\_evolution ()  
    (*pyRVEA.EAs.baseEA.BaseDecompositionEA method*), 4  
continue\_iteration ()  
    (*pyRVEA.EAs.baseEA.BaseDecompositionEA method*), 4  
create\_new\_individuals ()  
    (*pyRVEA.Population.Population.Population method*), 10

## E

eval\_fitness () (*pyRVEA.Population.Population.Population method*), 10  
evaluate\_individual ()  
    (*pyRVEA.Population.Population.Population method*), 10  
evolve () (*pyRVEA.Population.Population.Population method*), 10

## G

get\_extreme\_points\_c ()     (*in module pyRVEA.Selection.NSGAIII\_select*), 12  
get\_nadir\_point ()     (*in module pyRVEA.Selection.NSGAIII\_select*), 12

## H

householder ()     (*in module pyRVEA.OtherTools.ReferenceVectors*), 6  
hypervolume () (*pyRVEA.Population.Population.Population method*), 10

## I

IsNotebook ()     (*in module pyRVEA.OtherTools.IsNotebook*), 5

iteractive\_adapt\_1 ()

(*pyRVEA.OtherTools.ReferenceVectors.ReferenceVector*, 5) *pyRVEA.Recombination* (*module*), 12  
*pyRVEA.Selection.APD\_select* (*module*), 12  
*pyRVEA.Selection.NSGAIII\_select* (*module*), 12

## K

keep () (*pyRVEA.Population.Population.Population*, 10)

## M

mate () (*pyRVEA.Population.Population.Population*, 10)

## N

neighbouring\_angles ()

(*pyRVEA.OtherTools.ReferenceVectors.ReferenceVector*, 5) *pyRVEA.Recombination* (*module*)  
*pyRVEA.Selection.NSGAIII\_select* (12)

niching () (in module *pyRVEA.Selection.NSGAIII\_select*), 12

non\_dominated () (*pyRVEA.Population.Population.Population*, 10)

normalize () (in module *pyRVEA.OtherTools.ReferenceVectors*), 6

normalize () (*pyRVEA.OtherTools.ReferenceVectors.ReferenceVector*, 5)

NSGAIII (*class in pyRVEA.EAs.NSGAIII*), 3

NSGAIII\_select () (in module *pyRVEA.Selection.NSGAIII\_select*), 12

## O

objectives () (*pyRVEA.Problem.baseProblem.baseProblem*, 11)

objectives () (*pyRVEA.Problem.testProblem.testProblem*, 11)

## P

plot\_init\_ () (*pyRVEA.Population.Population.Population*, 10)

plot\_objectives () (*pyRVEA.Population.Population.Population*, 10)

Population (*class in pyRVEA.Population.Population*), 9

pyRVEA.EAs.baseEA (*module*), 4

pyRVEA.EAs.NSGAIII (*module*), 3

pyRVEA.EAs.RVEA (*module*), 3

pyRVEA.OtherTools.IsNotebook (*module*), 5

pyRVEA.OtherTools.plotlyanimate (*module*), 7

pyRVEA.OtherTools.ReferenceVectors (*module*), 5

pyRVEA.Population.Population (*module*), 9

pyRVEA.Problem.baseProblem (*module*), 11

pyRVEA.Problem.testProblem (*module*), 11

## R

ReferenceVectors (*class in pyRVEA.OtherTools.ReferenceVectors*), 5

rotate () (in module *pyRVEA.OtherTools.ReferenceVectors*), 6

rotate\_toward () (in module *pyRVEA.OtherTools.ReferenceVectors*), 6

RVEA (*class in pyRVEA.EAs.RVEA*), 3

## S

select () (*pyRVEA.EAs.baseEA.BaseDecompositionEA*, 4)

select () (*pyRVEA.EAs.NSGAIII.NSGAIII* method), 3

select () (*pyRVEA.EAs.RVEA.RVEA* method), 3

set\_params () (*pyRVEA.EAs.baseEA.BaseEA*, 5)

set\_params () (*pyRVEA.EAs.NSGAIII.NSGAIII* method), 3

set\_params () (*pyRVEA.EAs.RVEA.RVEA* method), 4

shear () (in module *pyRVEA.OtherTools.ReferenceVectors*), 6

slow\_interactive\_adapt () (*pyRVEA.OtherTools.ReferenceVectors.ReferenceVector*, 5)

## T

test () (in module *pyRVEA.OtherTools.plotlyanimate*), 9

test2 () (in module *pyRVEA.OtherTools.plotlyanimate*), 9

testProblem (*class in pyRVEA.Problem.testProblem*), 11

## U

update () (*pyRVEA.Problem.baseProblem.baseProblem*, 11)

update\_ideal\_and\_nadir () (*pyRVEA.Population.Population.Population*, 11)